

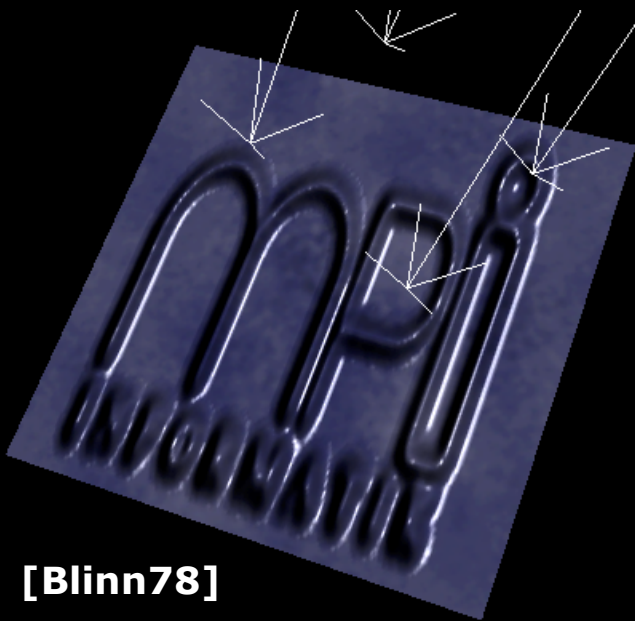
# **Towards Interactive Bump Mapping with Anisotropic Shift- Variant BRDFs**

**Jan Kautz**  
**Hans-Peter Seidel**



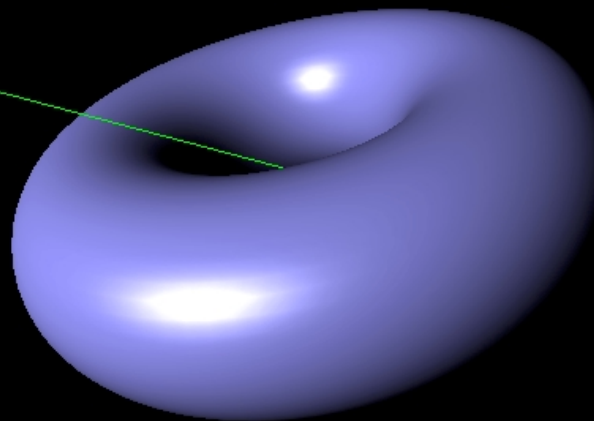
# Motivation

## Incompatible techniques:



[Blinn78]

**Bump Mapping  
(Phong model)**



[Heidrich99]

**Rendering with arbitrary BRDFs**

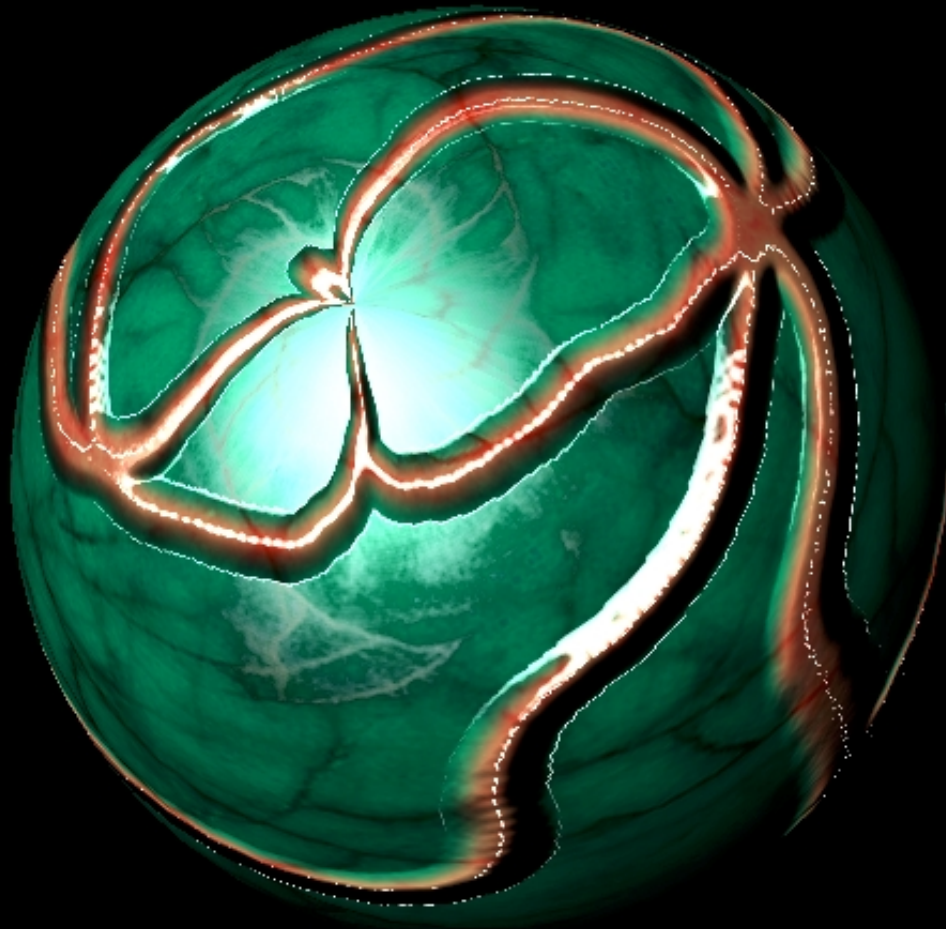


[Kautz99]

⇒ **Combine bump mapping & shift-variant BRDFs**

# Motivation

## Combine bump mapping & shift-variant BRDFs



### Per-pixel:

- Evaluation of BRDF
- BRDF parameters
- Normal and tangent

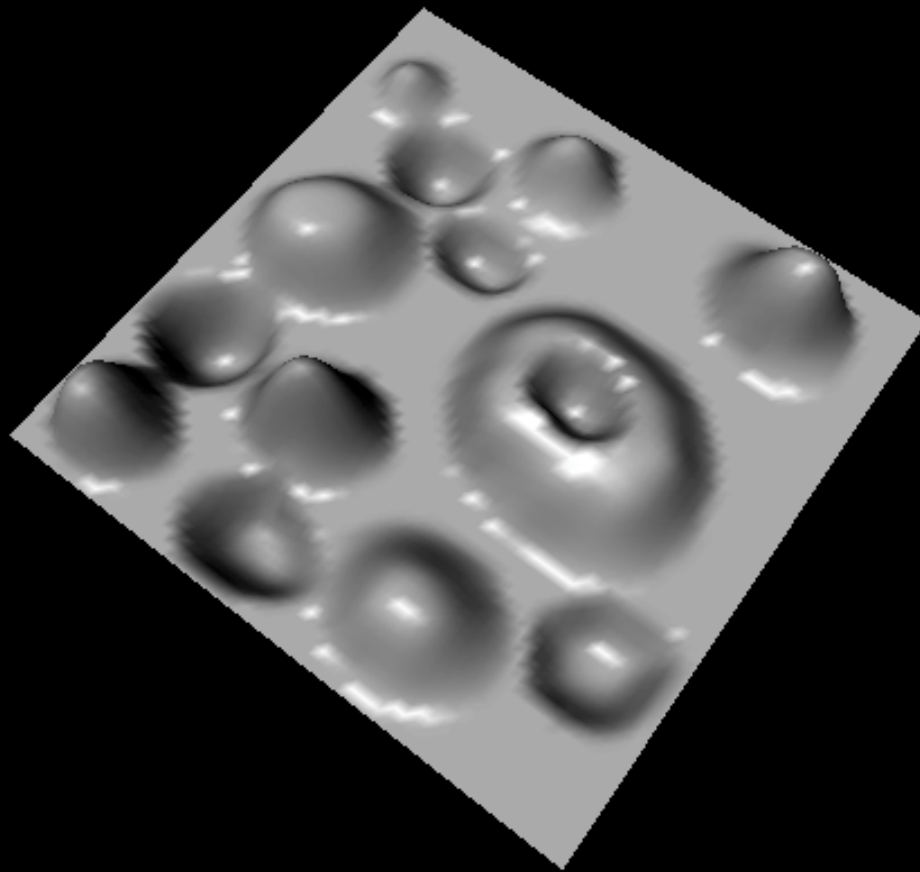
### Useful for e.g.:

- Human skin
- Corroded metal
- ...

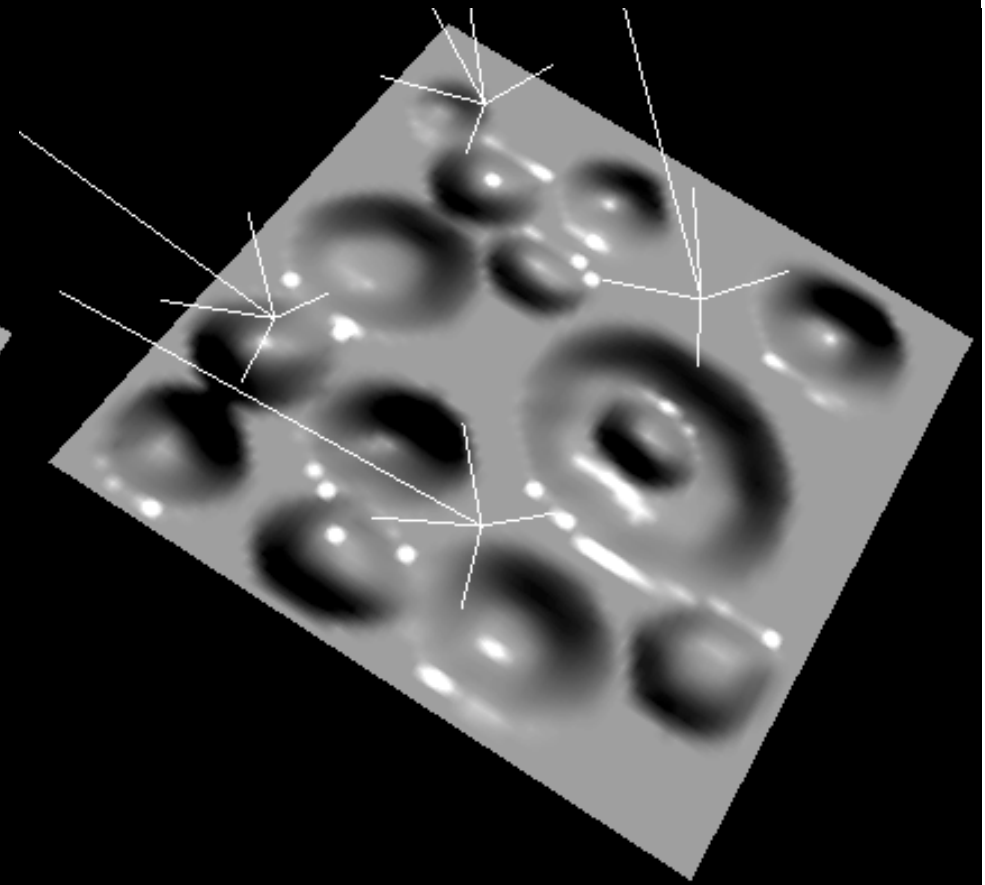
# Overview

- Introduction
  - Bump mapping
  - Reflectance models
  - Hardware capabilities
- Mapping reflectance models to hardware
- Examples
- Results
- Issues
- Conclusion

# Introduction - Bump Mapping



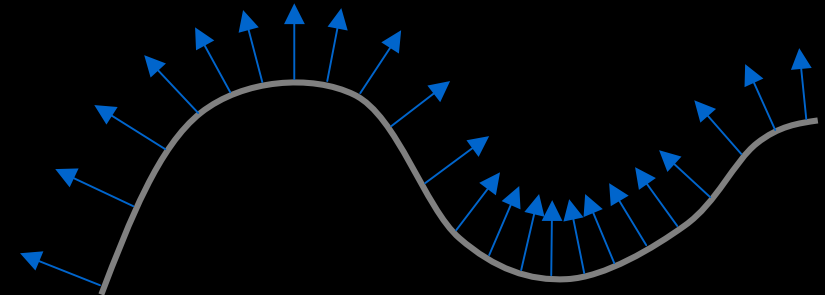
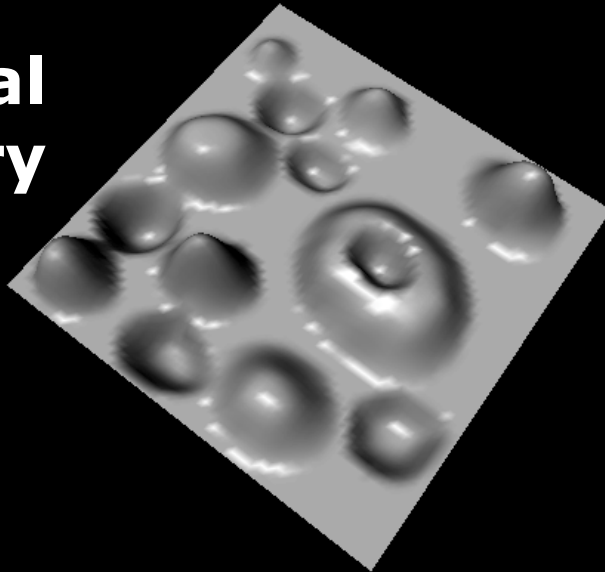
Real Geometry



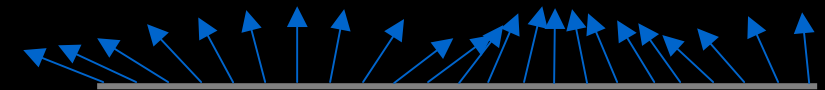
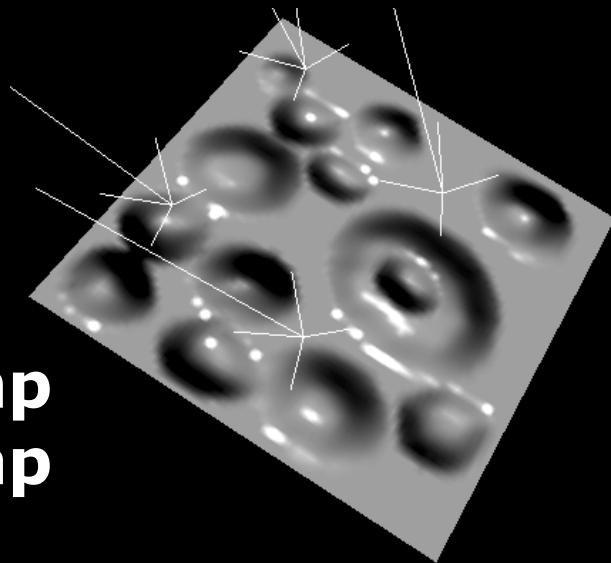
Bump Map

# Introduction - Bump Mapping

Real  
Geometry



Bump  
Map

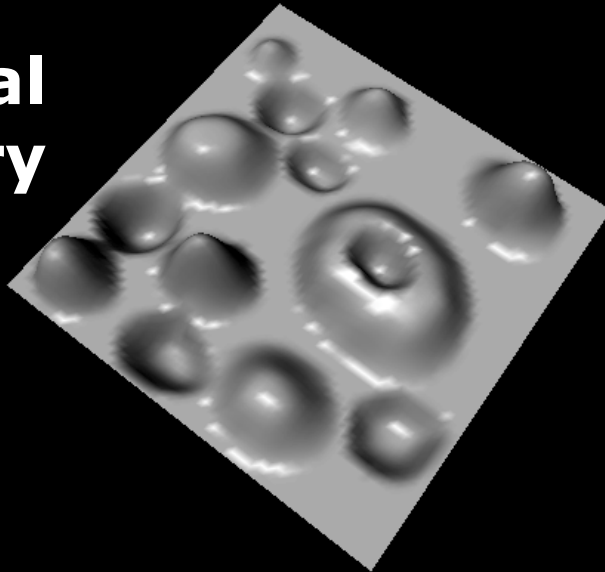


**Illumination:**

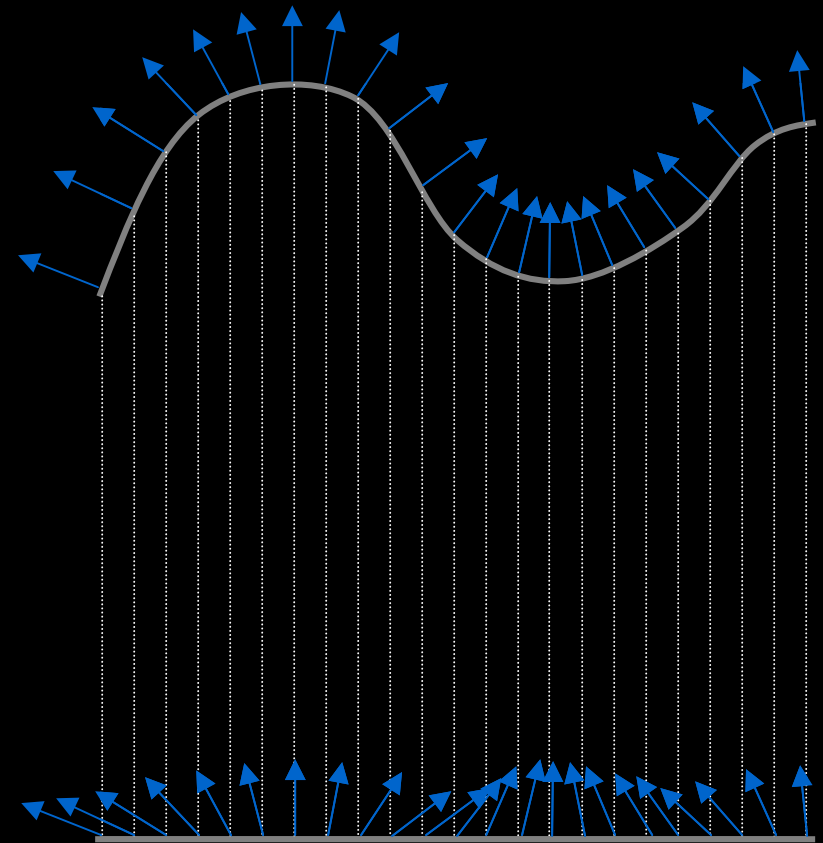
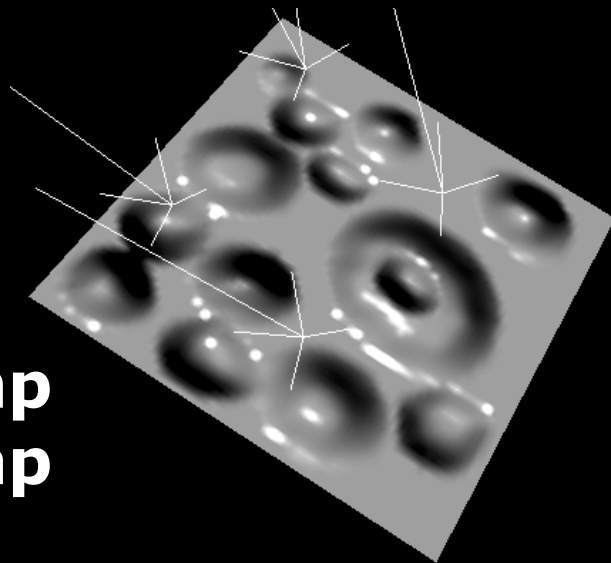
$$L_0 = k_s (\hat{h} \cdot \hat{n})^N + k_d (\hat{n} \cdot \hat{l})$$

# Introduction - Bump Mapping

Real  
Geometry



Bump  
Map

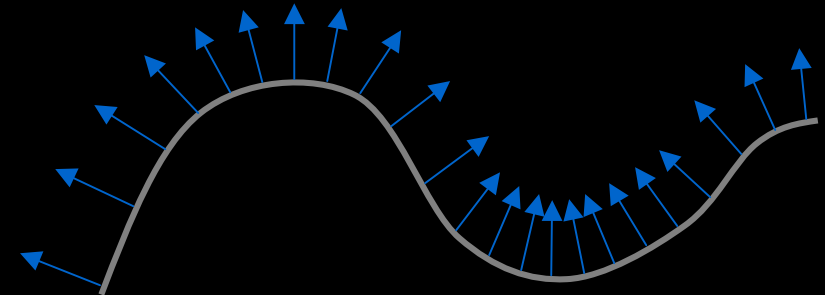
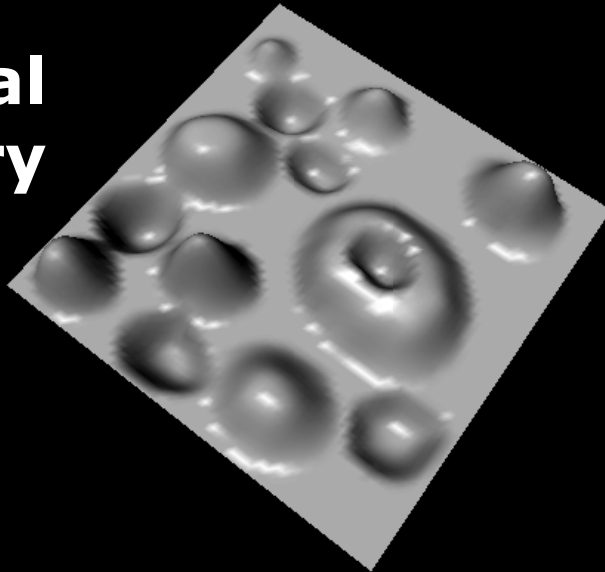


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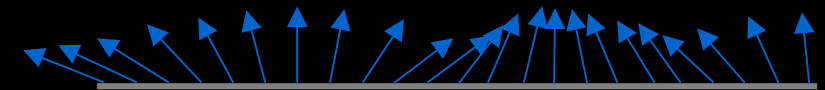
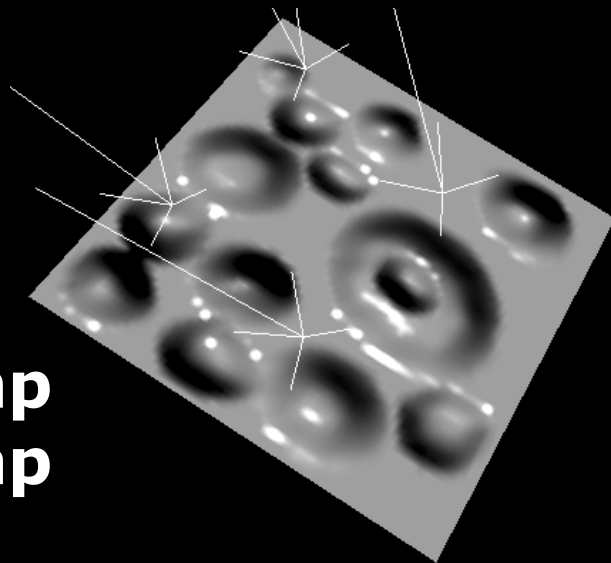
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# Introduction - Bump Mapping

Real  
Geometry



Bump  
Map



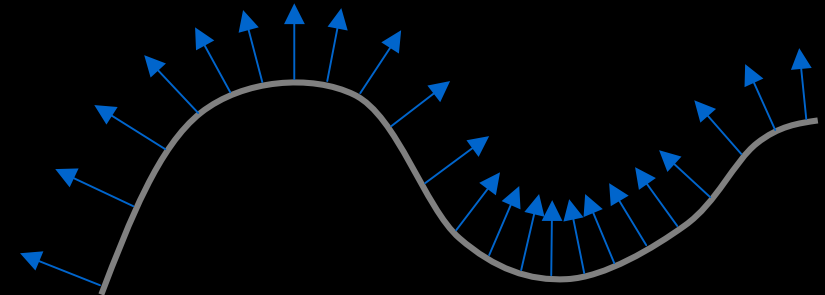
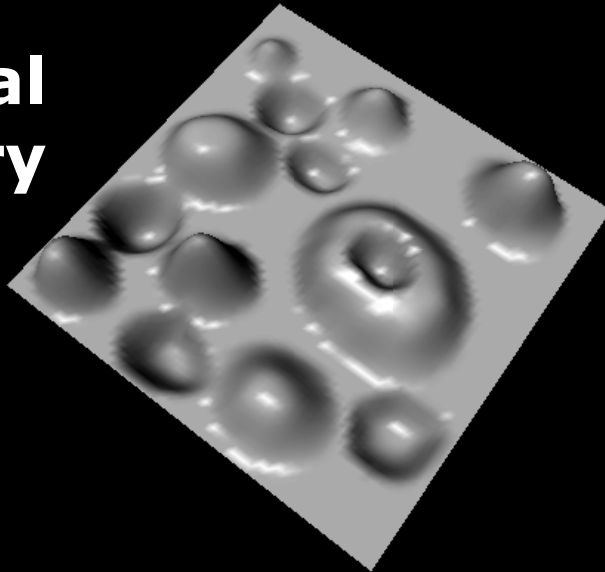
**Illumination:**

$$L_0 = k_s (\hat{h} \cdot \hat{n})^N + k_d (\hat{n} \cdot \hat{l})$$

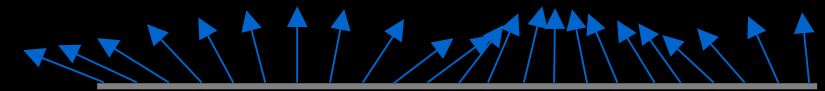
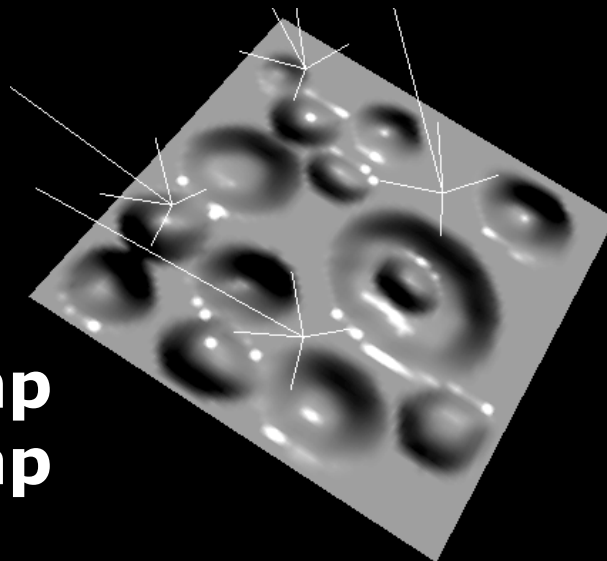


# Introduction - Bump Mapping

Real  
Geometry



Bump  
Map

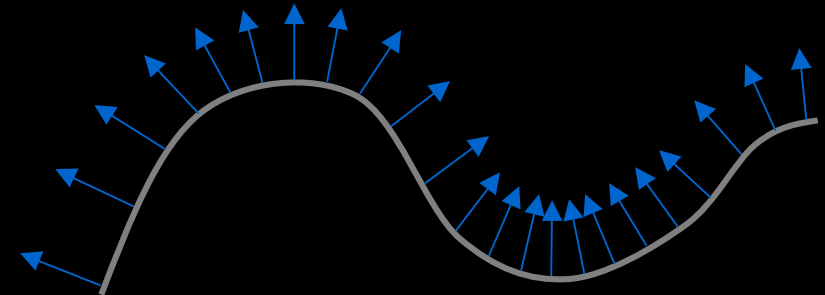
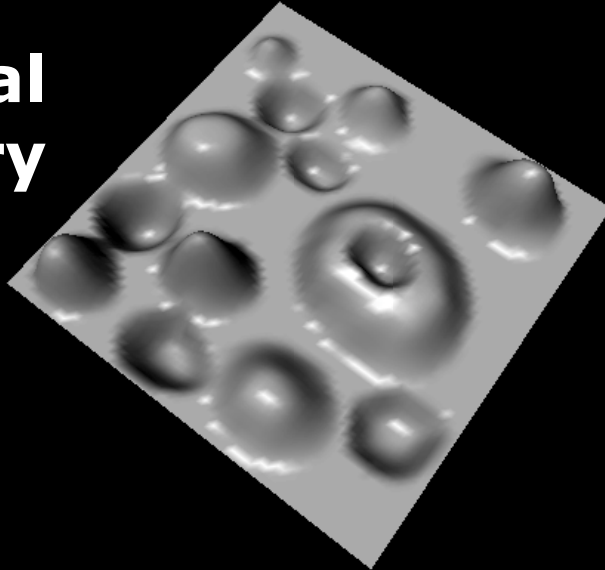


Illumination:

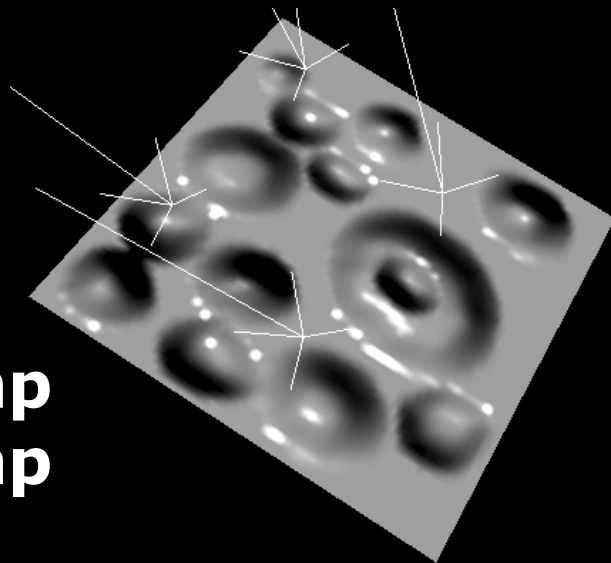
$$L_0 = k_s (\hat{h} \cdot \hat{n})^N + k_d (\hat{n} \cdot \hat{l})$$

# Introduction - Bump Mapping

Real  
Geometry



Bump  
Map

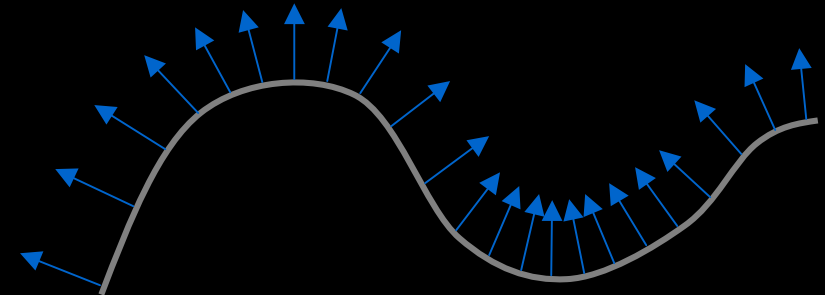
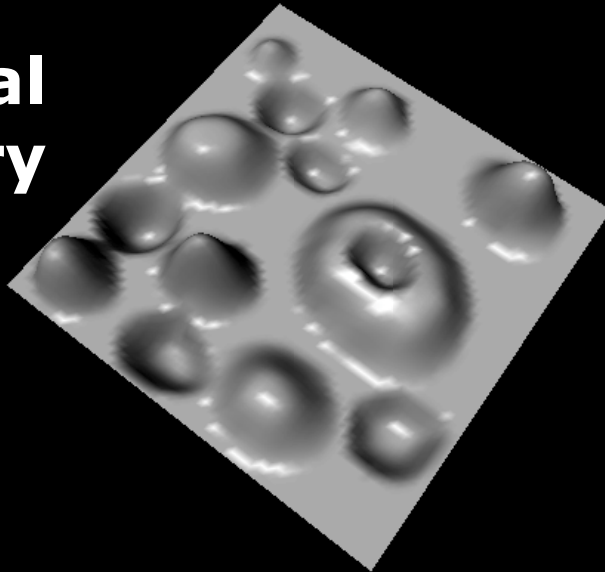


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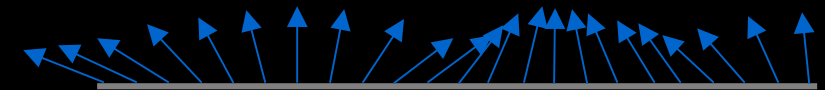
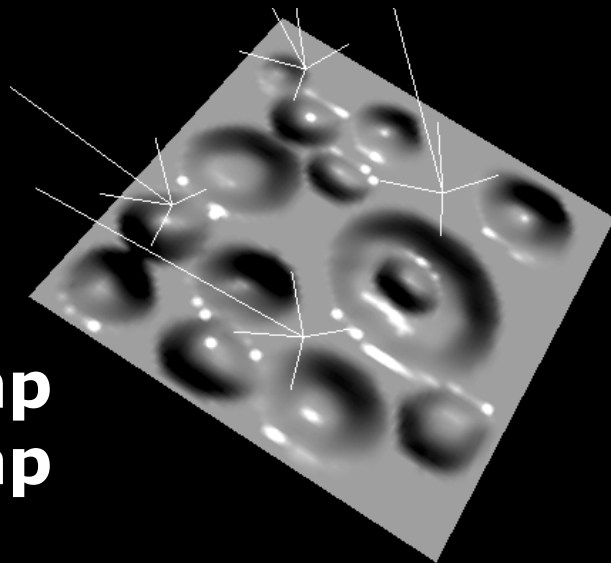
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# Introduction - Bump Mapping

Real  
Geometry



Bump  
Map

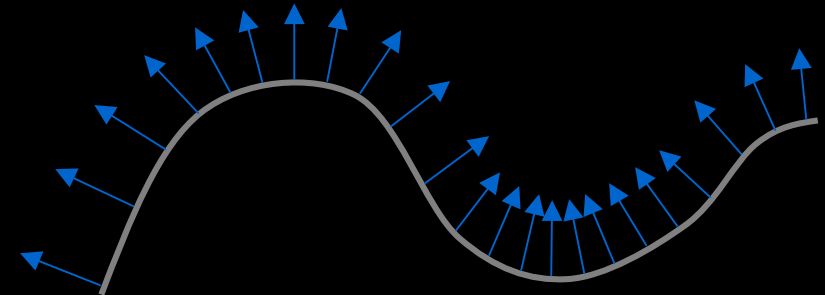
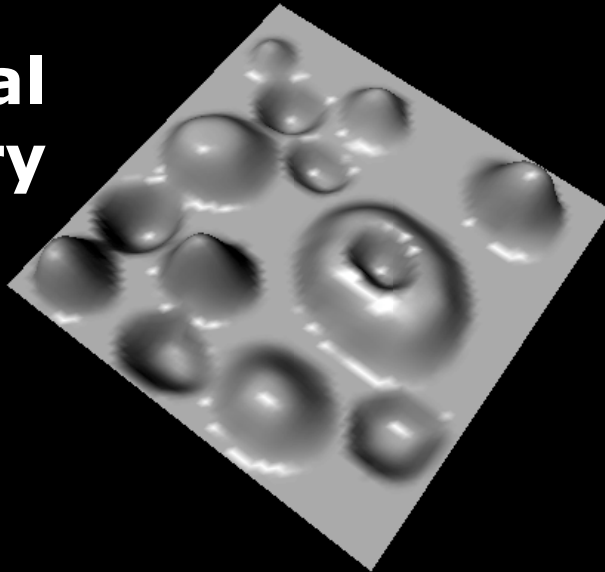


Illumination:

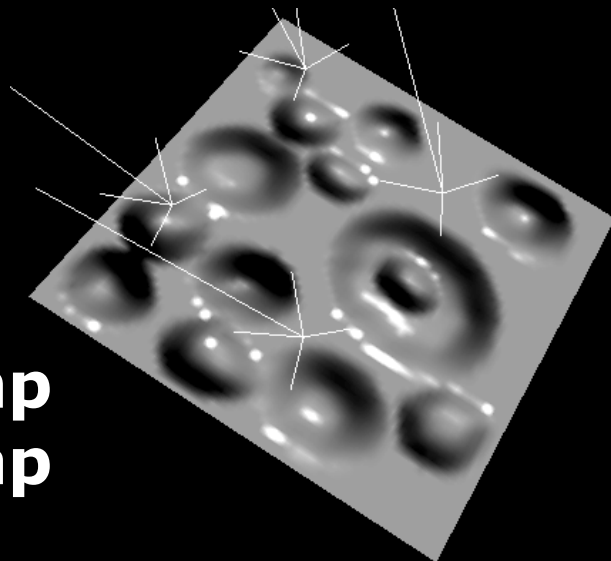
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# Introduction - Bump Mapping

Real  
Geometry



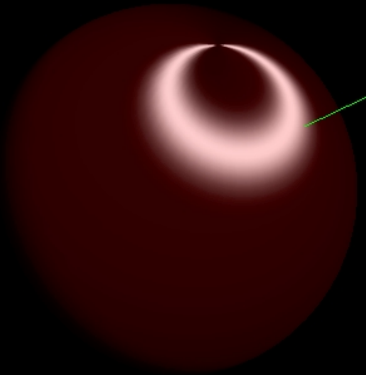
Bump  
Map



Illumination:

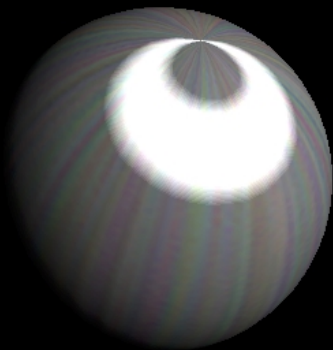
$$L_0 = k_s (\hat{h} \cdot \hat{n})^N + k_d (\hat{n} \cdot \hat{l})$$

# Introduction – Reflectance Models



**Banks:**

$$L_0 = k_s (\hat{n} \cdot \hat{l}) \left( \sqrt{1 - (\hat{v} \cdot \hat{t})^2} \sqrt{1 - (\hat{l} \cdot \hat{t})^2} - (\hat{v} \cdot \hat{t})(\hat{l} \cdot \hat{t}) \right)$$



**Anisotropic Blinn-Phong:**

$$L_0 = k_s \sqrt{1 - \left( \hat{h} \cdot \frac{\hat{t}}{\alpha_x} \right)^2 - \left( \hat{h} \cdot \frac{\hat{b}}{\alpha_y} \right)^2}^N$$



**Ward:**

$$L_0 = \frac{k_s (\hat{n} \cdot \hat{l})}{\sqrt{(\hat{l} \cdot \hat{n})(\hat{v} \cdot \hat{n})}} \frac{1}{4\pi\alpha_x\alpha_y} e^{\left( \frac{-2}{1 + \hat{h} \cdot \hat{n}} \left( \left( \frac{\hat{h} \cdot \hat{t}}{\alpha_x} \right)^2 + \left( \frac{\hat{h} \cdot \hat{b}}{\alpha_y} \right)^2 \right) \right)}$$

# Hardware Capabilities

## Modern graphics hardware has per-pixel:

- Addition and subtraction
- Multiplication
- Dot-product
- Extended range  $[-1:1]$

⇒ **Not enough for complex reflectance models!**

# Dependent Texturing

Colors of 1<sup>st</sup> texture map serve as texture coordinates of 2<sup>nd</sup> texture map:



Mathematically:  $f : (u, v) \rightarrow (R, G, B)$

⇒ **Allows arbitrary functions**

# Mapping Reflectance Models to Hardware

## Idea:

- Decompose reflectance model into:  
**supported** and **unsupported** operations
- Use per-pixel operations for supported ops
- Use dependent texturing for unsupported operations/functions
- Put BRDF parameters into texture maps

## Two phases:

- Precalculation (for unsupported operations)
- Rendering



# Precalculation

## Example: Anisotropic Blinn-Phong

$$L_0 = k_s \sqrt[2N]{1 - \left( \hat{h} \cdot \frac{\hat{t}}{\alpha_x} \right)^2 - \left( \hat{h} \cdot \frac{\hat{b}}{\alpha_y} \right)^2}$$

**decompose**

$$G(s, t) = \sqrt{s}^t$$

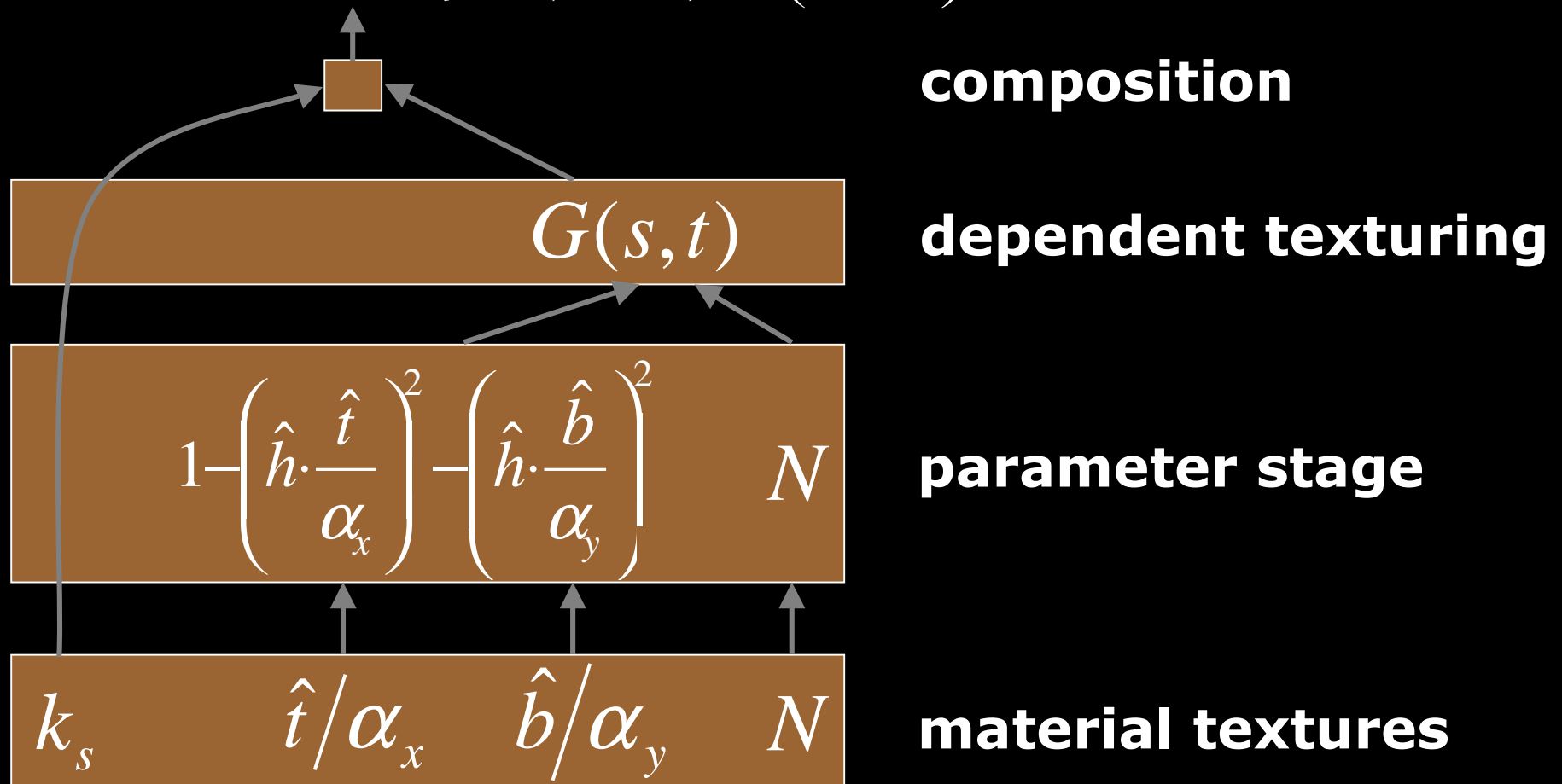
**put into textures**

$$G(s, t) :$$



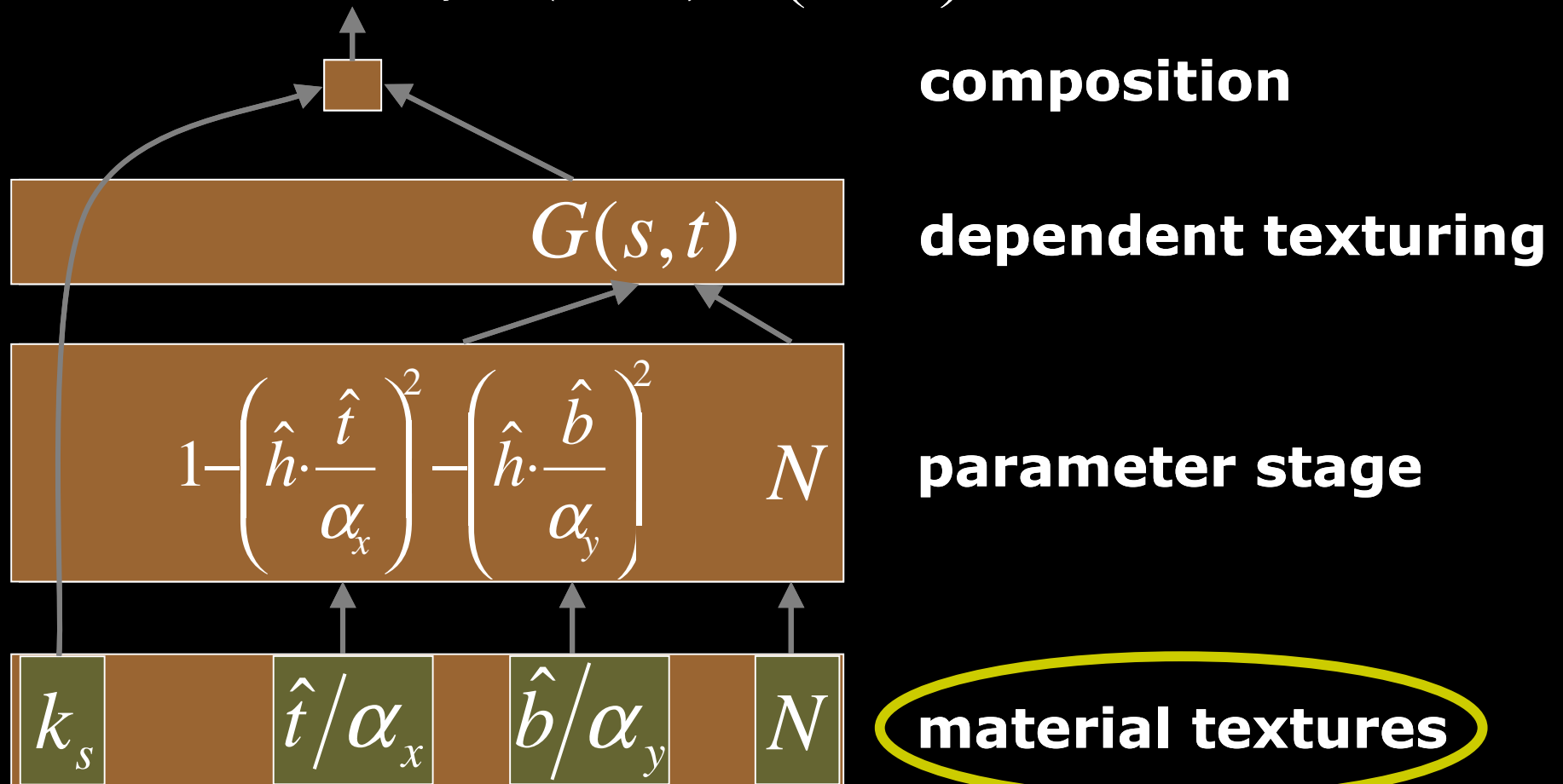
# Rendering

$$L_0 = k_s \sqrt{1 - \left( \hat{h} \cdot \frac{\hat{t}}{\alpha_x} \right)^2 - \left( \hat{h} \cdot \frac{\hat{b}}{\alpha_y} \right)^2}^N$$



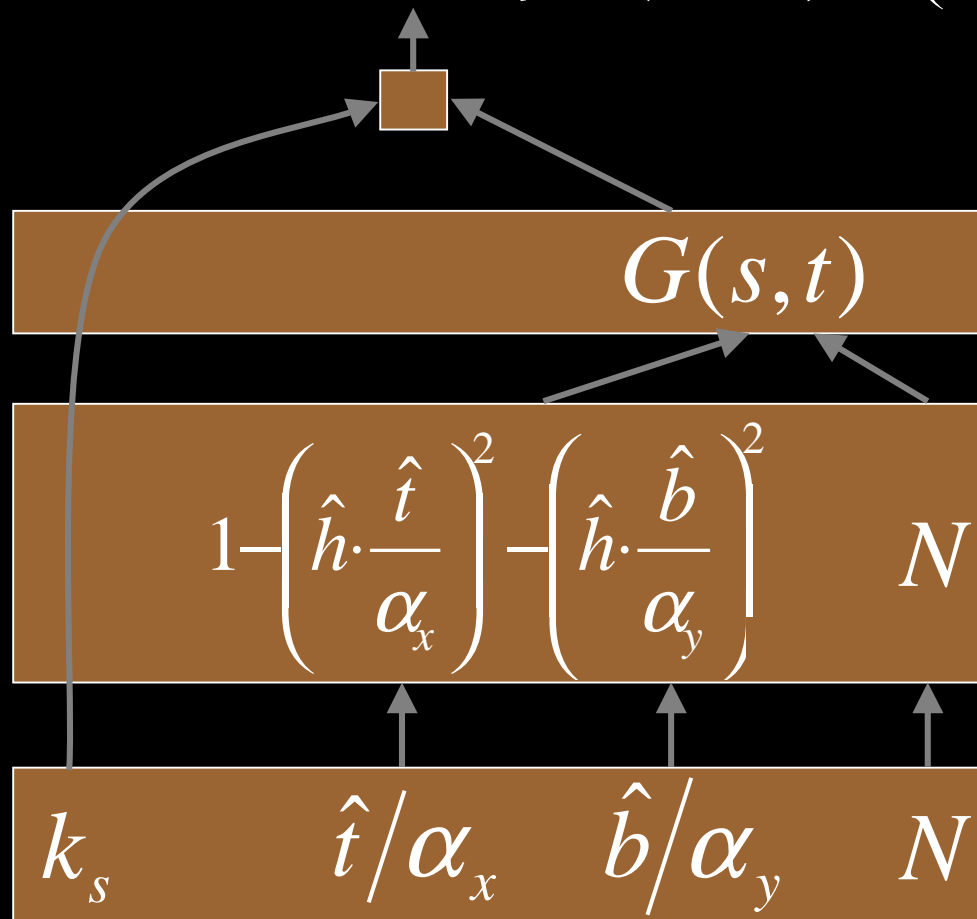
# Rendering

$$L_0 = k_s \sqrt{1 - \left( \hat{h} \cdot \frac{\hat{t}}{\alpha_x} \right)^2 - \left( \hat{h} \cdot \frac{\hat{b}}{\alpha_y} \right)^2}^N$$



# Rendering

$$L_0 = k_s \sqrt{1 - \left( \hat{h} \cdot \frac{\hat{t}}{\alpha_x} \right)^2 - \left( \hat{h} \cdot \frac{\hat{b}}{\alpha_y} \right)^2}^N$$



**composition**

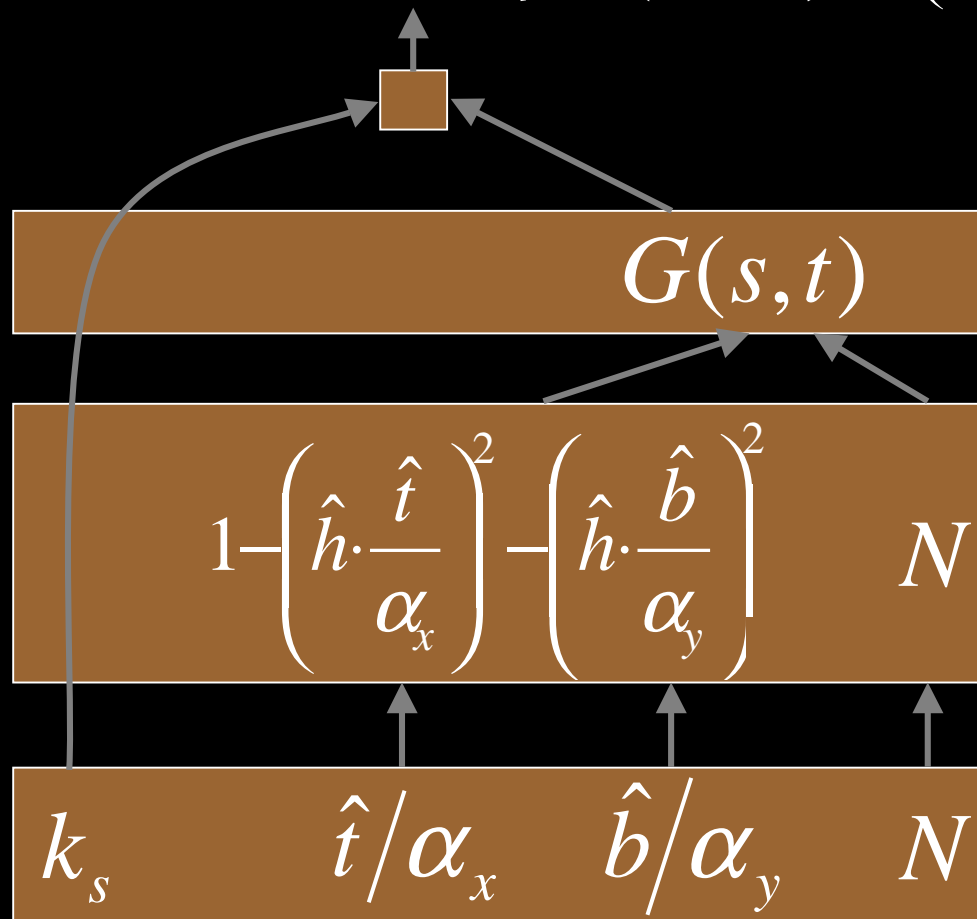
**dependent texturing**

**parameter stage**

**material textures**

# Rendering

$$L_0 = k_s \sqrt{1 - \left( \hat{h} \cdot \frac{\hat{t}}{\alpha_x} \right)^2 - \left( \hat{h} \cdot \frac{\hat{b}}{\alpha_y} \right)^2}^N$$



**composition**

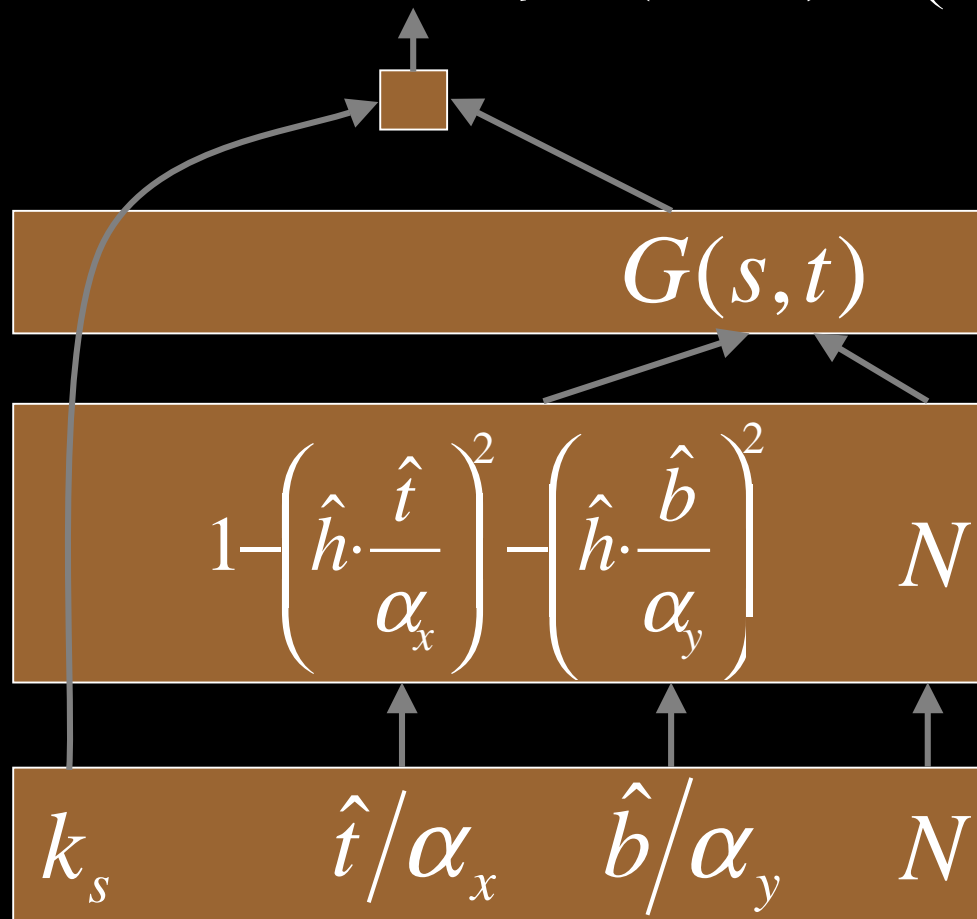
**dependent texturing**

**parameter stage**

**material textures**

# Rendering

$$L_0 = k_s \sqrt{1 - \left( \hat{h} \cdot \frac{\hat{t}}{\alpha_x} \right)^2 - \left( \hat{h} \cdot \frac{\hat{b}}{\alpha_y} \right)^2}^N$$



**composition**

**dependent texturing**

**parameter stage**

**material textures**

# Rendering

$$L_0 = k_s \sqrt{1 - \left( \hat{h} \cdot \frac{\hat{t}}{\alpha_x} \right)^2 - \left( \hat{h} \cdot \frac{\hat{b}}{\alpha_y} \right)^2}^N$$

**composition**

$$G(s, t)$$

**dependent texturing**

$$1 - \left( \hat{h} \cdot \frac{\hat{t}}{\alpha_x} \right)^2 - \left( \hat{h} \cdot \frac{\hat{b}}{\alpha_y} \right)^2 \quad N$$

**parameter stage**

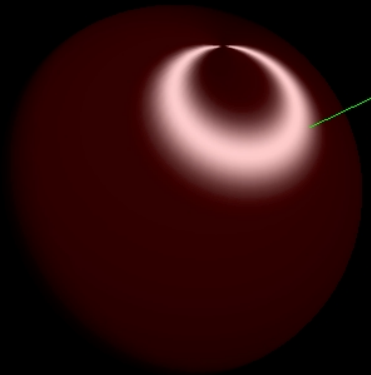
$$k_s \quad \hat{t}/\alpha_x \quad \hat{b}/\alpha_y \quad N$$

**material textures**

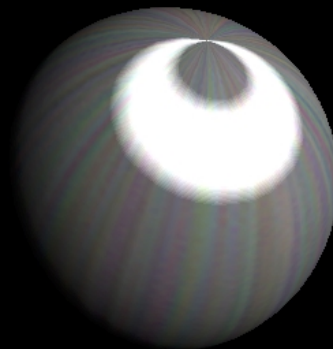
# Other Models

**Works with most analytical models**

**We have tried:**



**Banks**



**Anisotropic  
Blinn-Phong**



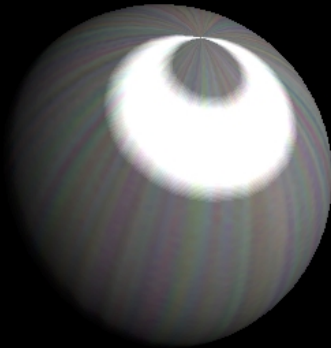
**Ward**



# Results

## Rendering are done with:

- Modified anisotropic Blinn-Phong model:



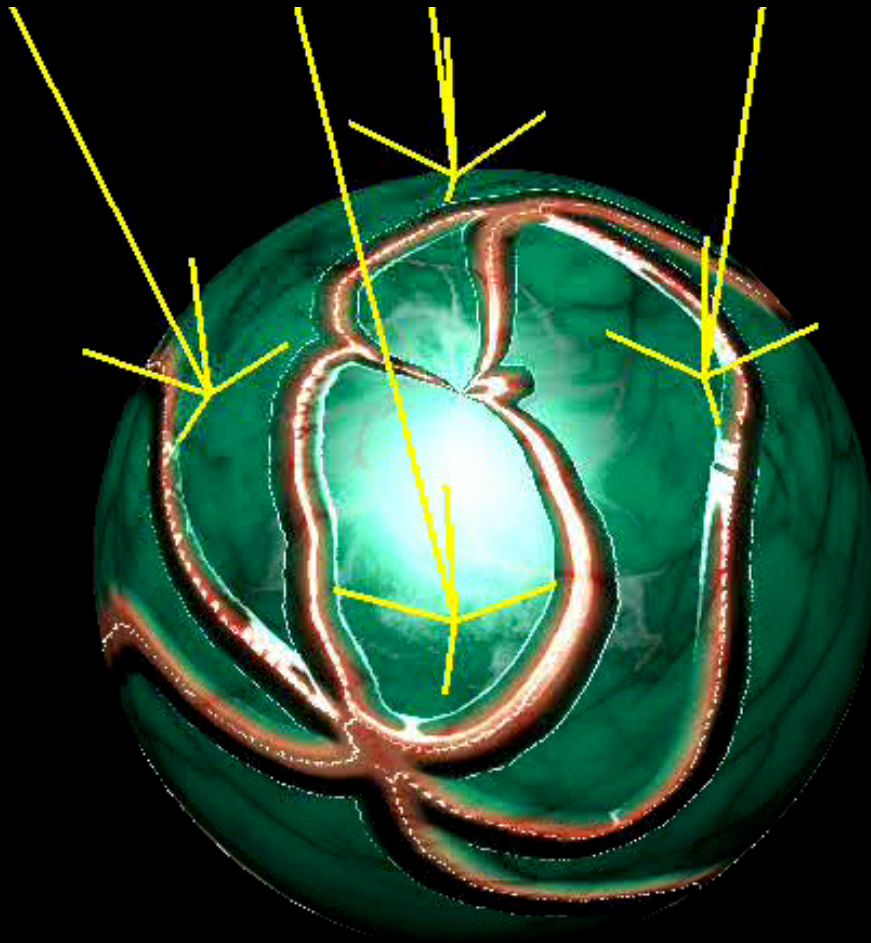
$$L_0 = k_s \left( 1 - \left( \hat{h} \cdot \frac{\hat{t}}{\alpha_x} \right)^2 - \left( \hat{h} \cdot \frac{\hat{b}}{\alpha_y} \right)^2 \right)$$

- On a GeForce 256 using register combiners

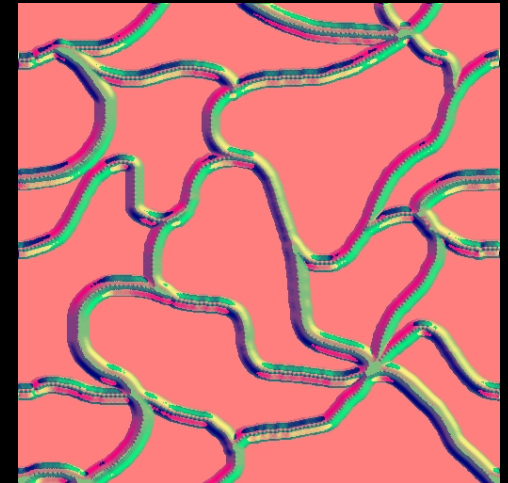
(Also works on SGIs using color matrix)

# Results – Anisotropic Blinn-Phong

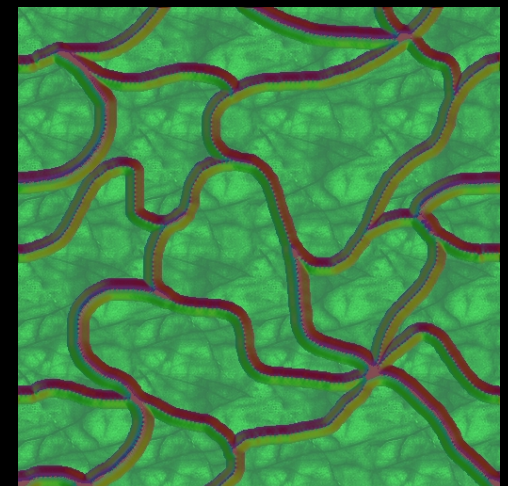
Material textures:



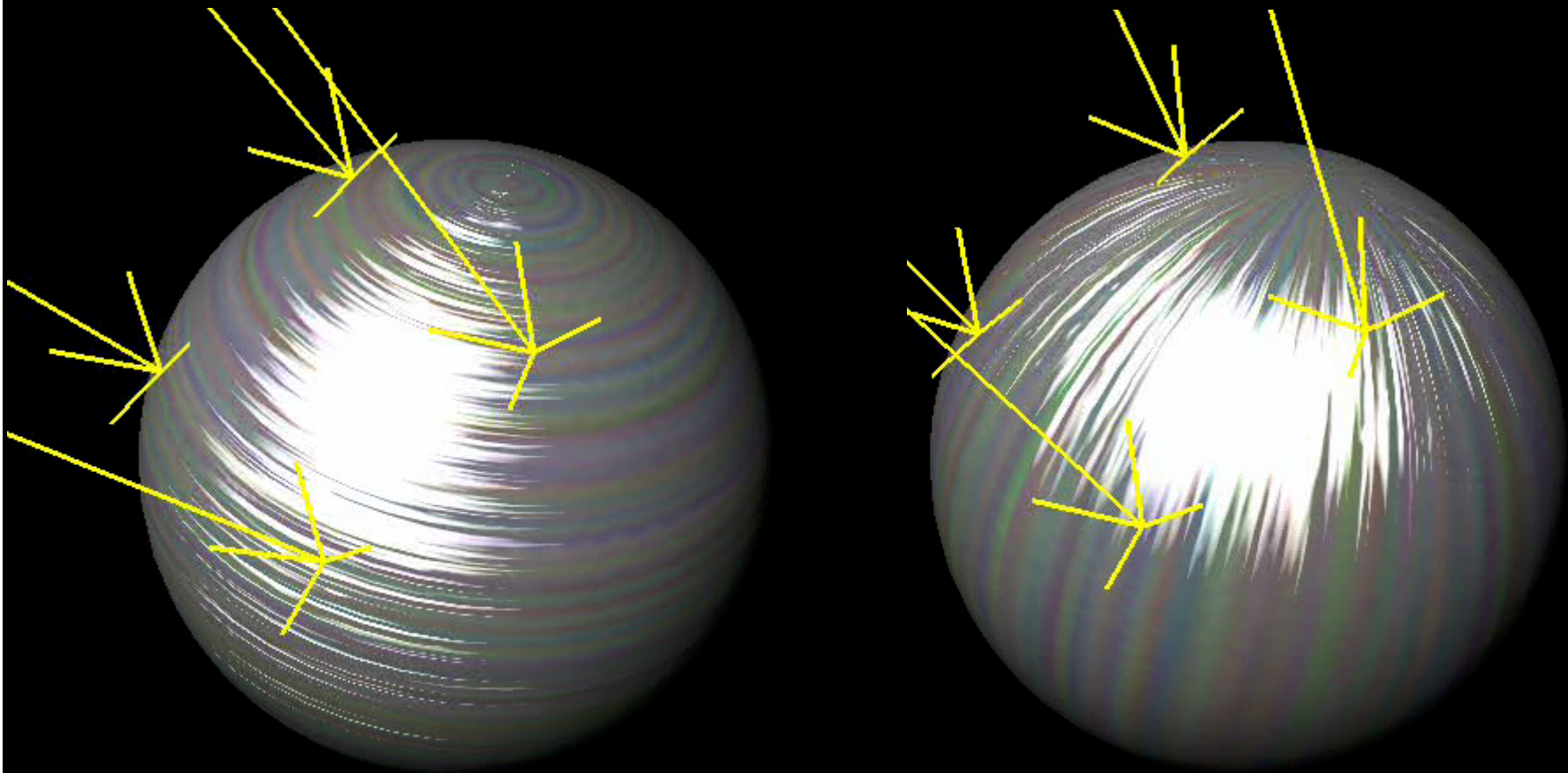
$$\frac{\hat{t}}{\alpha_x} :$$



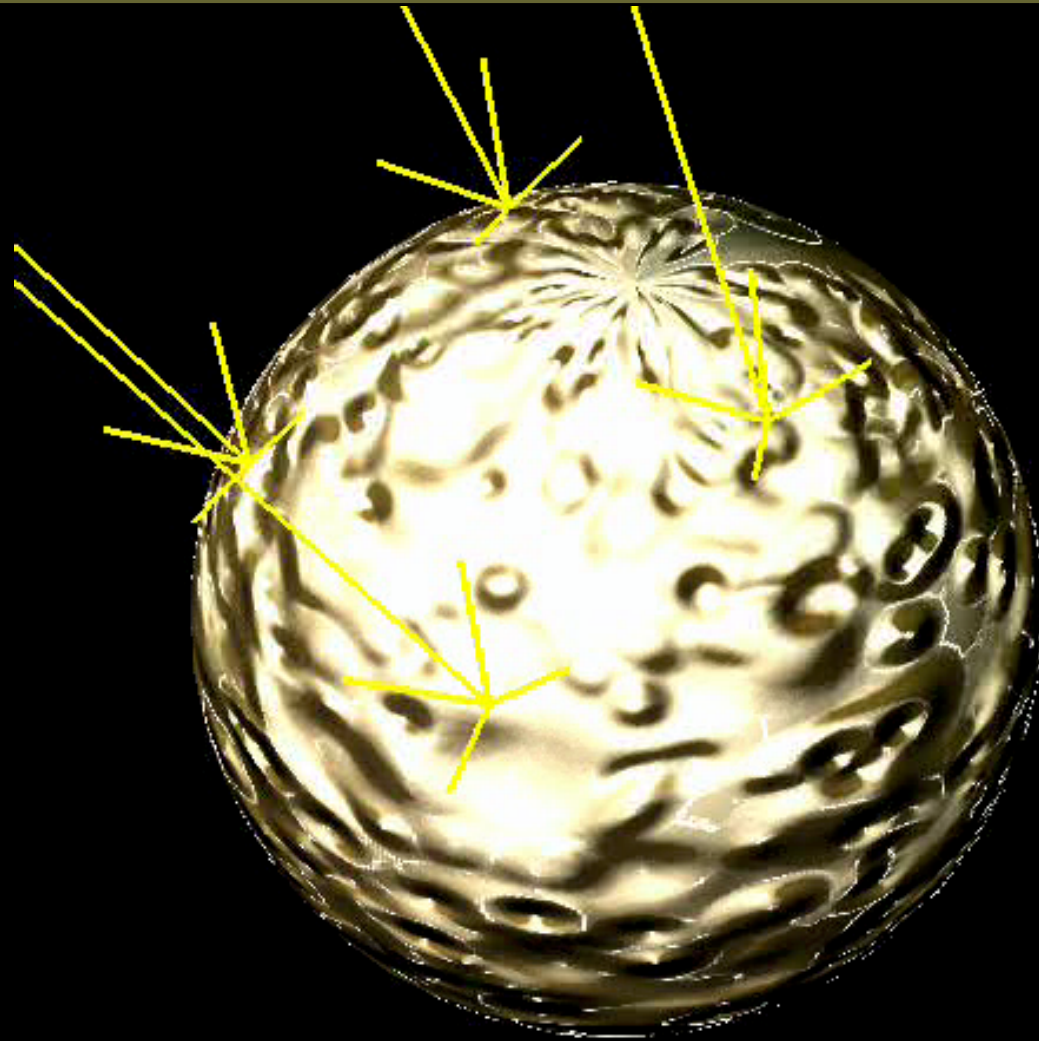
$$\frac{\hat{b}}{\alpha_y} :$$



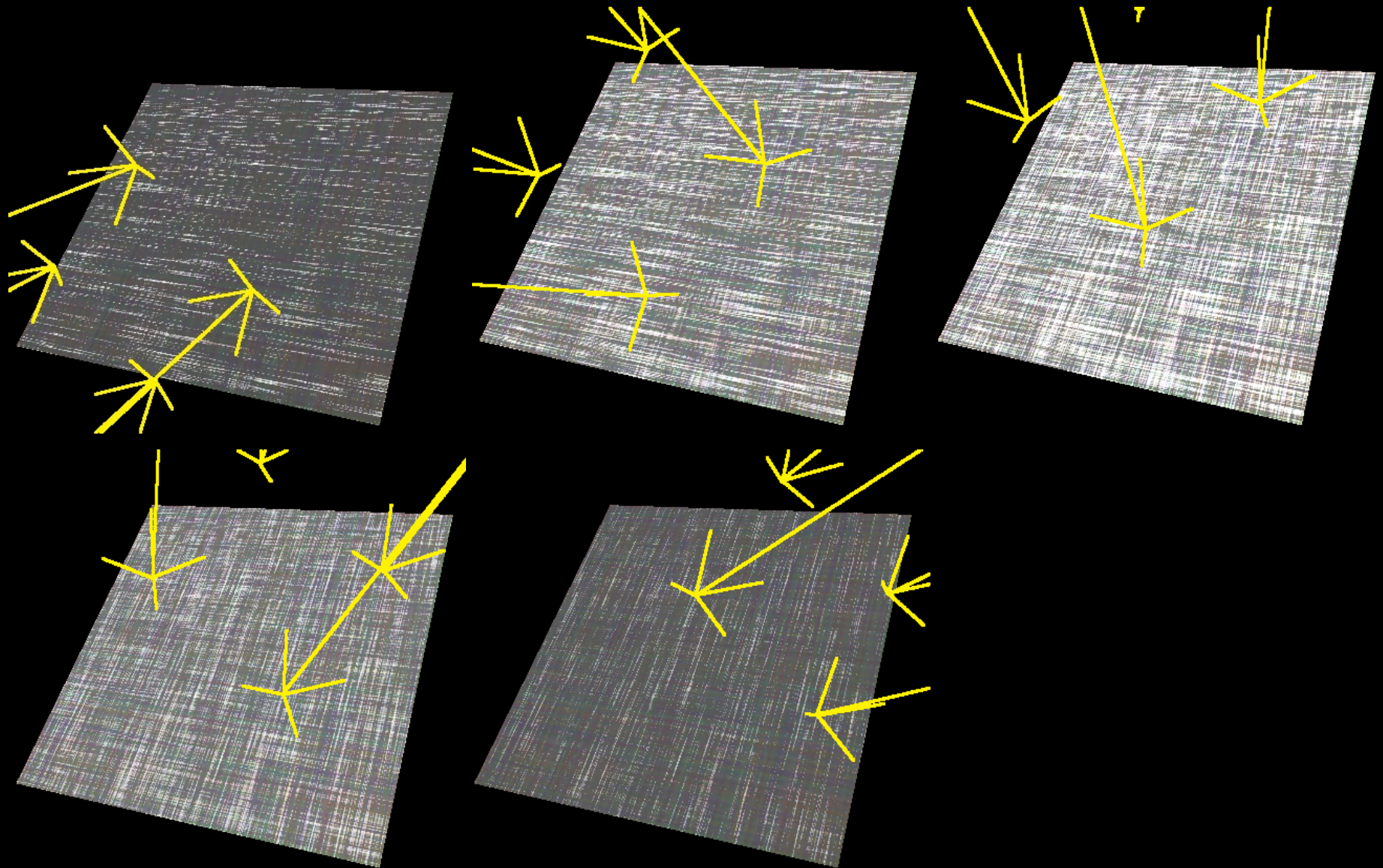
# Results



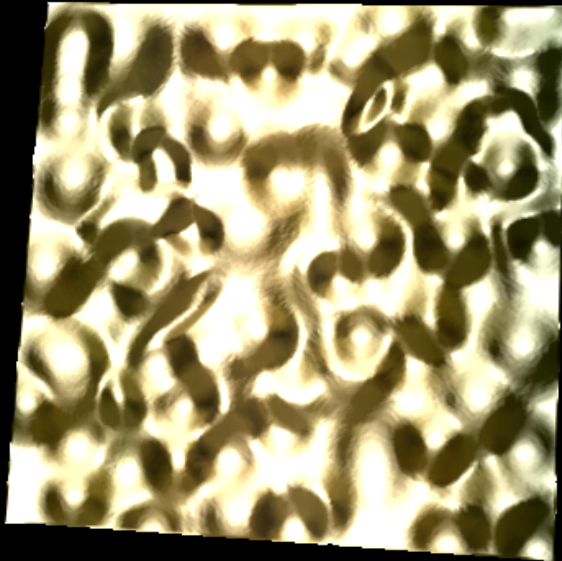
# Results



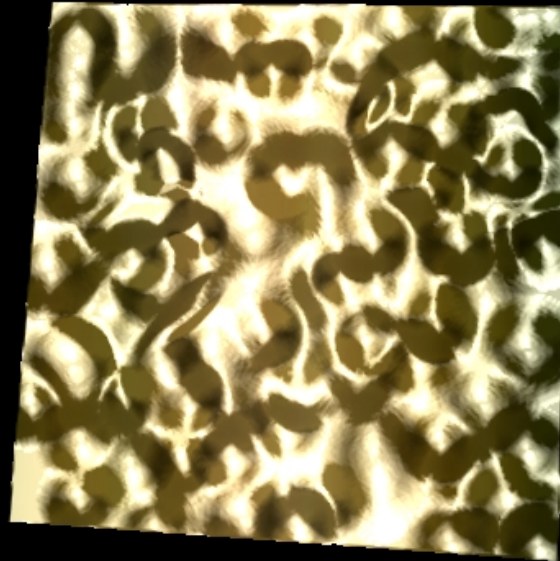
# Results



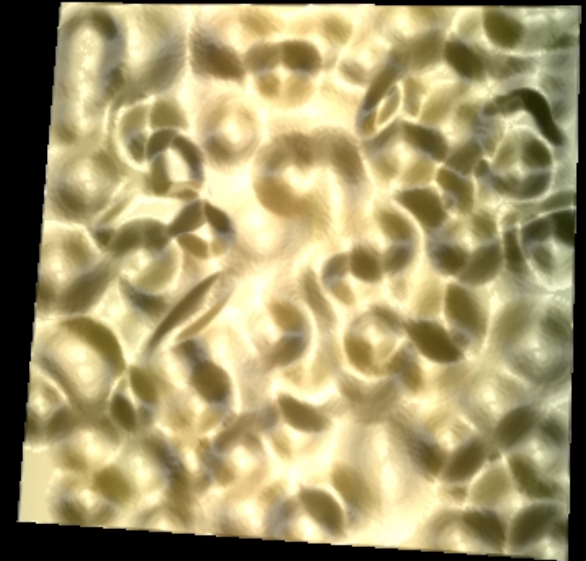
# Results



**Banks**

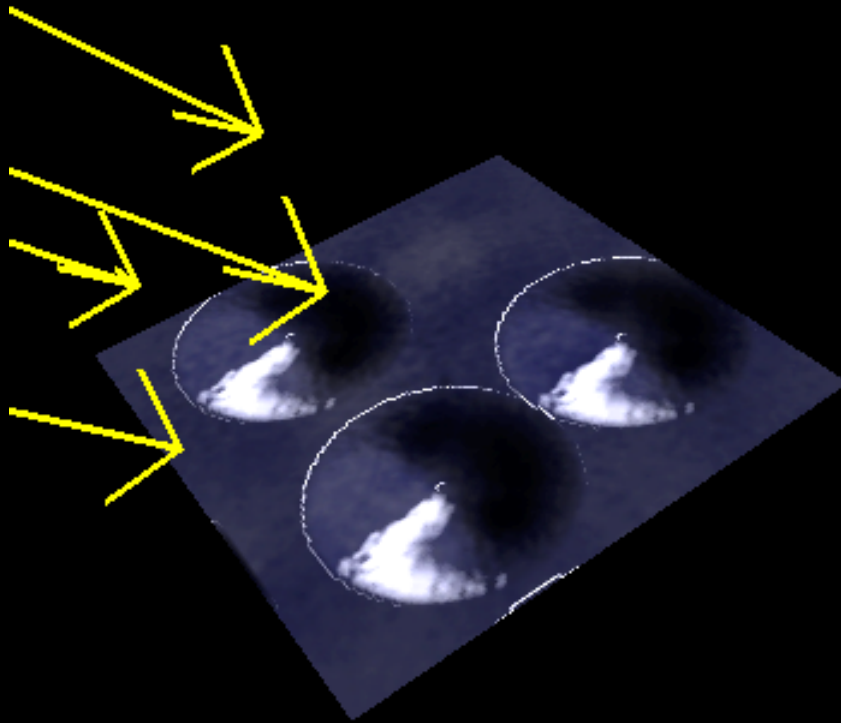


**Anisotropic  
Blinn-Phong**

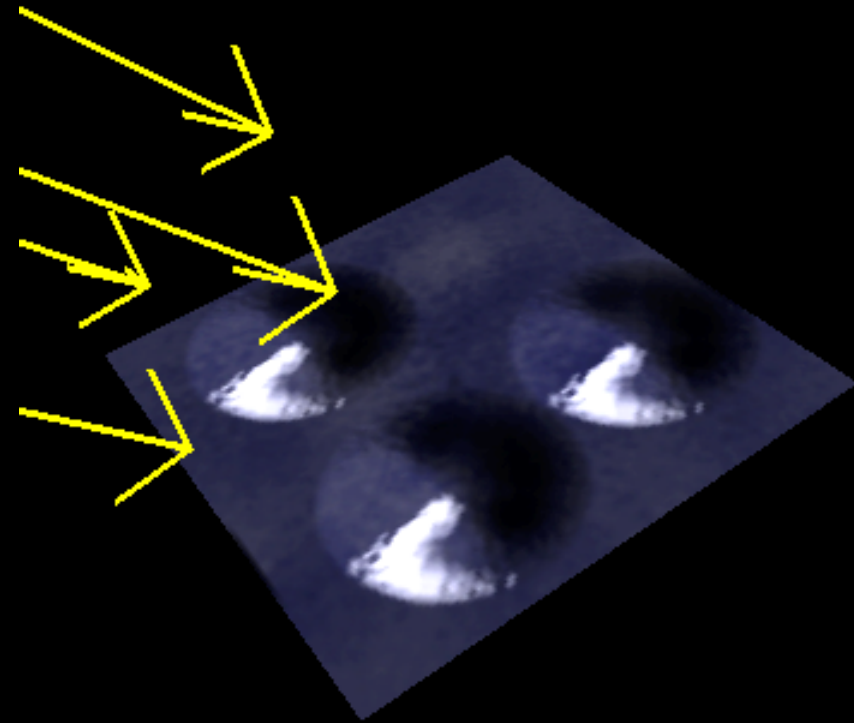


**Ward**

# Issues



**NVIDIA register  
combiner**



**Software**

# Hardware Issues

## Bilinear Filtering of Textures:

- Filtering happens before fed into multi-texturing unit

## Dependent Texture Lookup:

- Expensive
- Likely not to happen *within* multi-texturing
- Not widely available (yet)



# Discussion

## Dependent Tex.

- Flexible
- Inconvenient to access
- Expensive to use (depends on data)

## Adding New Ops

- Which operations?
- Sqrt, Division, ... are *very* expensive
- Always something missing

⇒ **Adding new ops is orthogonal to Dependent Texturing**

# Conclusions

## Technique allows:

- Bump mapping *with*
- Many different
- Shift-Variant BRDFs

## Future Work:

- Mip-mapping to avoid aliasing
- Avoid bilinear filtering artefacts

# Questions?

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**Thank you!**

**<http://www.mpi-sb.mpg.de>**